



Efficient Sampling-design in Multistate Disease Process for Screening and Surveillance

Dr. Chen-Yang Hsu, Dr. Wen-Feng Hsu
Professor Hsiu-Hsi Chen

Division of Biostatistics, College of Public Health,
National Taiwan University



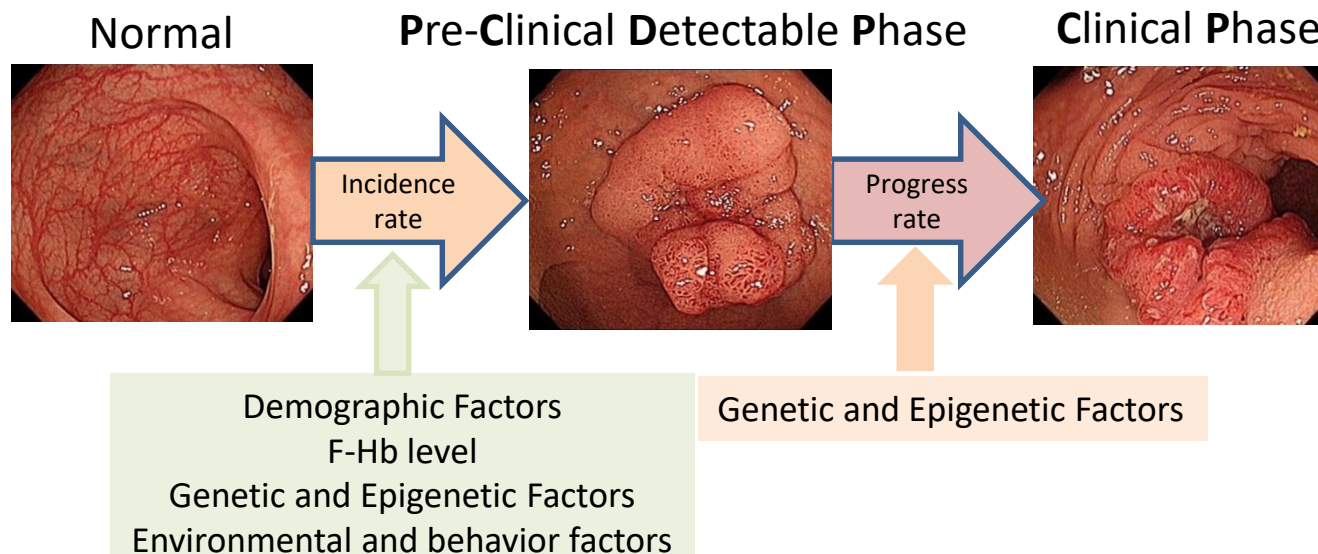
國立臺灣大學 公共衛生學院
College of Public Health National Taiwan University

Multistate Model and Disease progression

1. State-specific effect of multistate disease progression
2. State-specific effect of multistate disease progression
3. Risk- and State-based cancer prevention

$$\text{Efficacy} = 1 - \frac{O}{E}$$

O: observed rate of disease progression
E: expected rate of disease progression

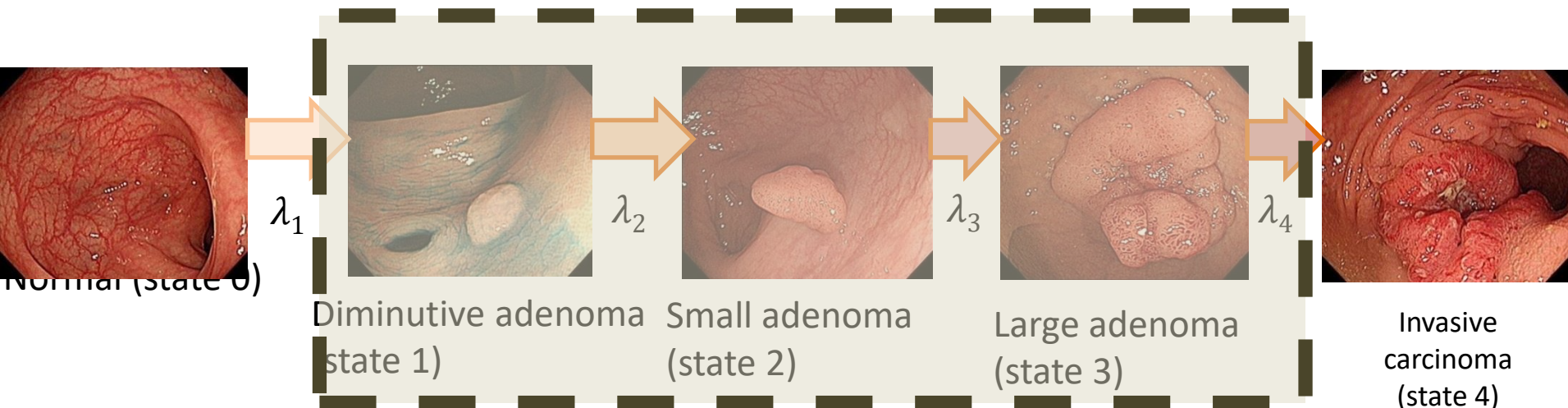


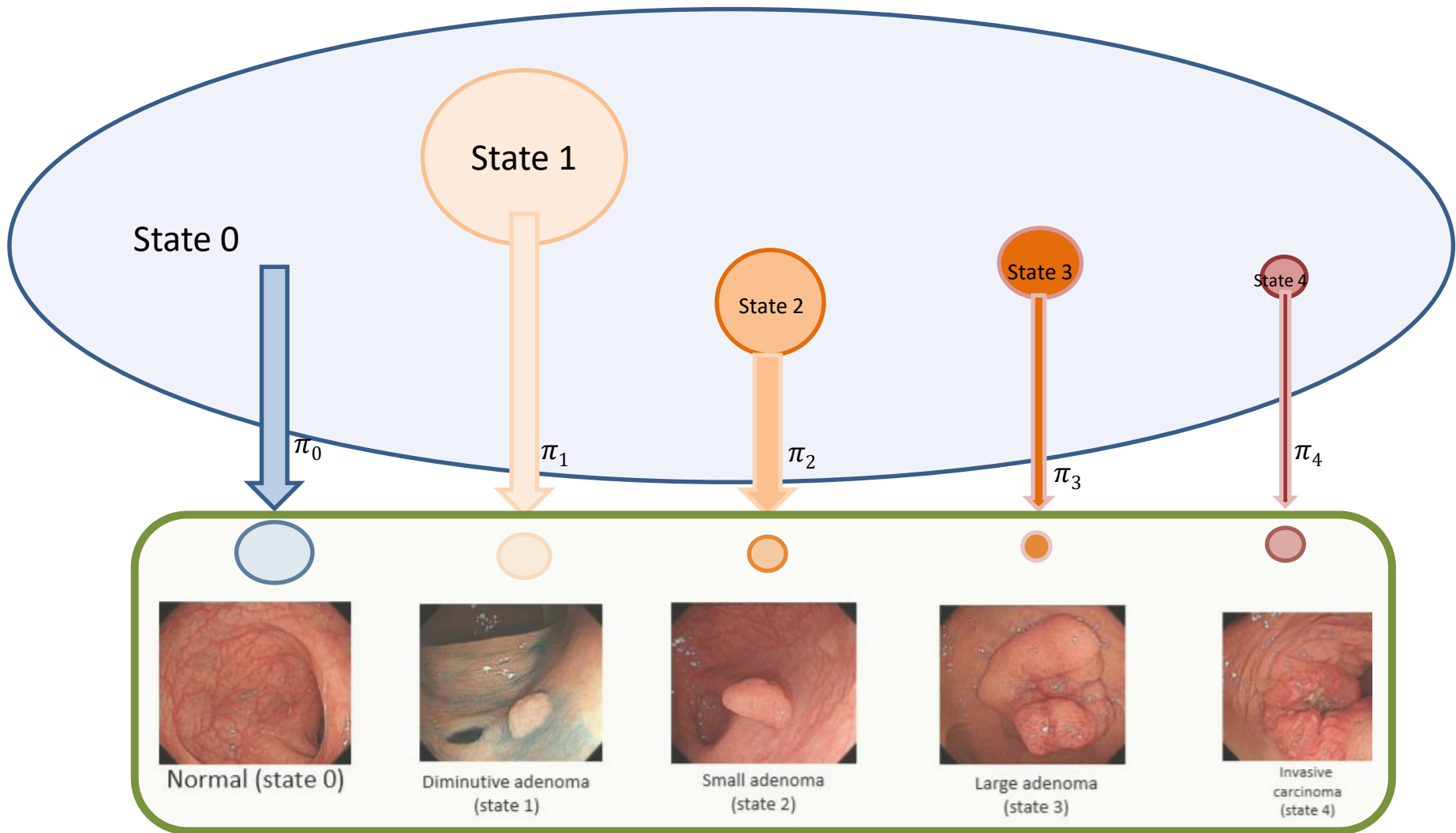
Stochastic model for non-standard case-cohort design

Tony Hsiu-Hsi Chen,^{*,†} Ming-Fang Yen, Ming-Neng Shiu,
Tao-Hsin Tung and Hui-Min Wu

*Institute of Preventive Medicine, College of Public Health, National Taiwan University,
Room 207, 19 Hsueh Road, Taipei 100, Taiwan*

1. Quantifying the rates of disease progression using **non-standard case-cohort design**
2. Assessing the **efficacy of polypectomy** according to disease characteristics





	Normal	(%)	Polyp	(%)	colorectal cancer	(%)
Cohort	10,496		2,652		760	
Sample	305	2.9	300	11.3	116	15.3

Disease progression and Sampling fraction

$$P(0 \rightarrow j, t_i | S = 1)$$

$$= \frac{P(S = 1 | 0 \rightarrow j, t_i) P(0 \rightarrow j, t_i)}{\sum_{j=1}^n P(S = 1 | 0 \rightarrow j, t_i) P(0 \rightarrow j, t_i)} = \frac{\pi_j P(0 \rightarrow j, t_i)}{\sum_{j=1}^n \pi_j P(0 \rightarrow j, t_i)} = \frac{\pi_j P_{0j}(t_i)}{\sum_{j=1}^n \pi_j P_{0j}(t_i)}$$

Likelihood function

$$\prod_i \left(\frac{\pi_0 P_{00}(t_i)}{\sum_{j=0}^4 \pi_j P_{0j}(t_i)} \right)^{n_{i0}} \left(\frac{\pi_1 P_{01}(t_i)}{\sum_{j=0}^4 \pi_j P_{0j}(t_i)} \right)^{n_{i1}} \left(\frac{\pi_2 P_{02}(t_i)}{\sum_{j=0}^4 \pi_j P_{0j}(t_i)} \right)^{n_{i2}} \left(\frac{\pi_3 P_{03}(t_i)}{\sum_{j=0}^4 \pi_j P_{0j}(t_i)} \right)^{n_{i3}} \times \left(\frac{\pi_4 P_{04}(t_i)}{\sum_{j=0}^4 \pi_j P_{0j}(t_i)} \right)^{n_{i4}}$$

$$\text{Efficacy} = 1 - O/E$$

O: observed rate of disease progression

E: expected rate of disease progression

Efficacy of Polypectomy

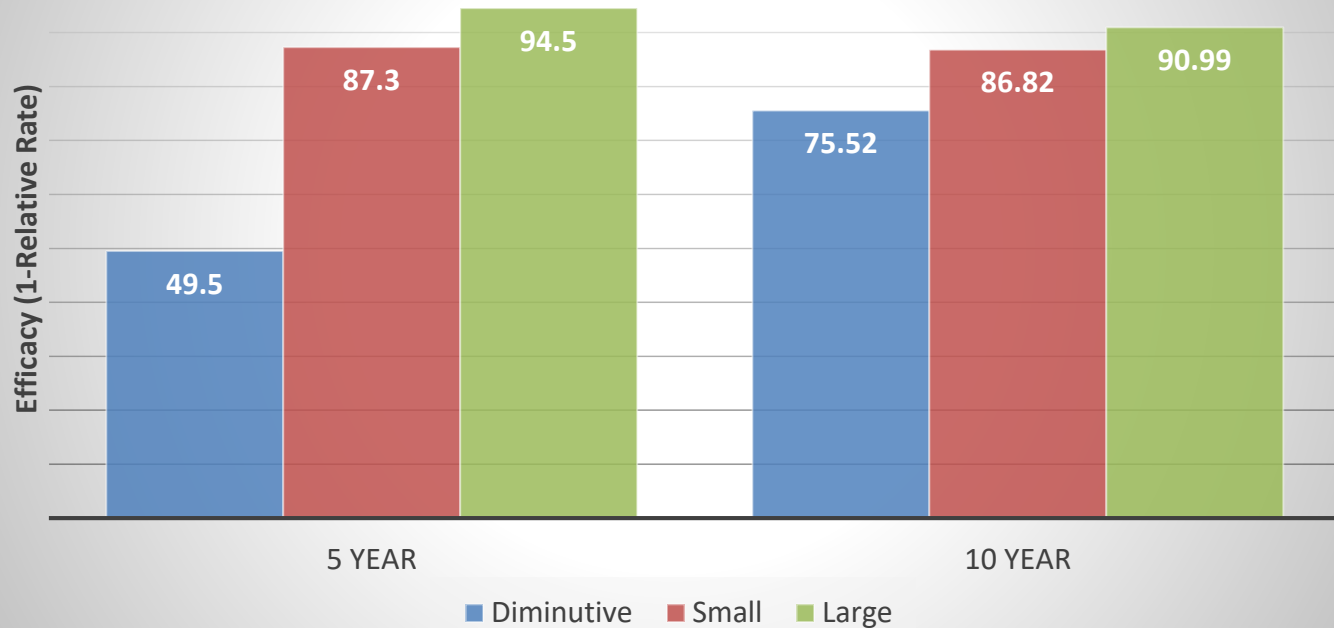


Table VI. Treatment efficacy of malignant transformation to colorectal cancer by adenoma size after 5-year and 10-year follow-up.

Adenoma size	Treatment efficacy	
	5 Year (per cent)	10 Year (per cent)
Diminutive	49.52	75.52
Small	87.31	86.82
Large	94.52	90.99



Multistate Markov Model with Two-stage Sampling Design

Aims

- Extend the **non-standard case-cohort design** from cross-sectional study to follow-up study
- Incorporation measurement error in the model
- Elucidate multistate disease progression
- Assess the state-specific effect of subject-specific characteristics with efficiency

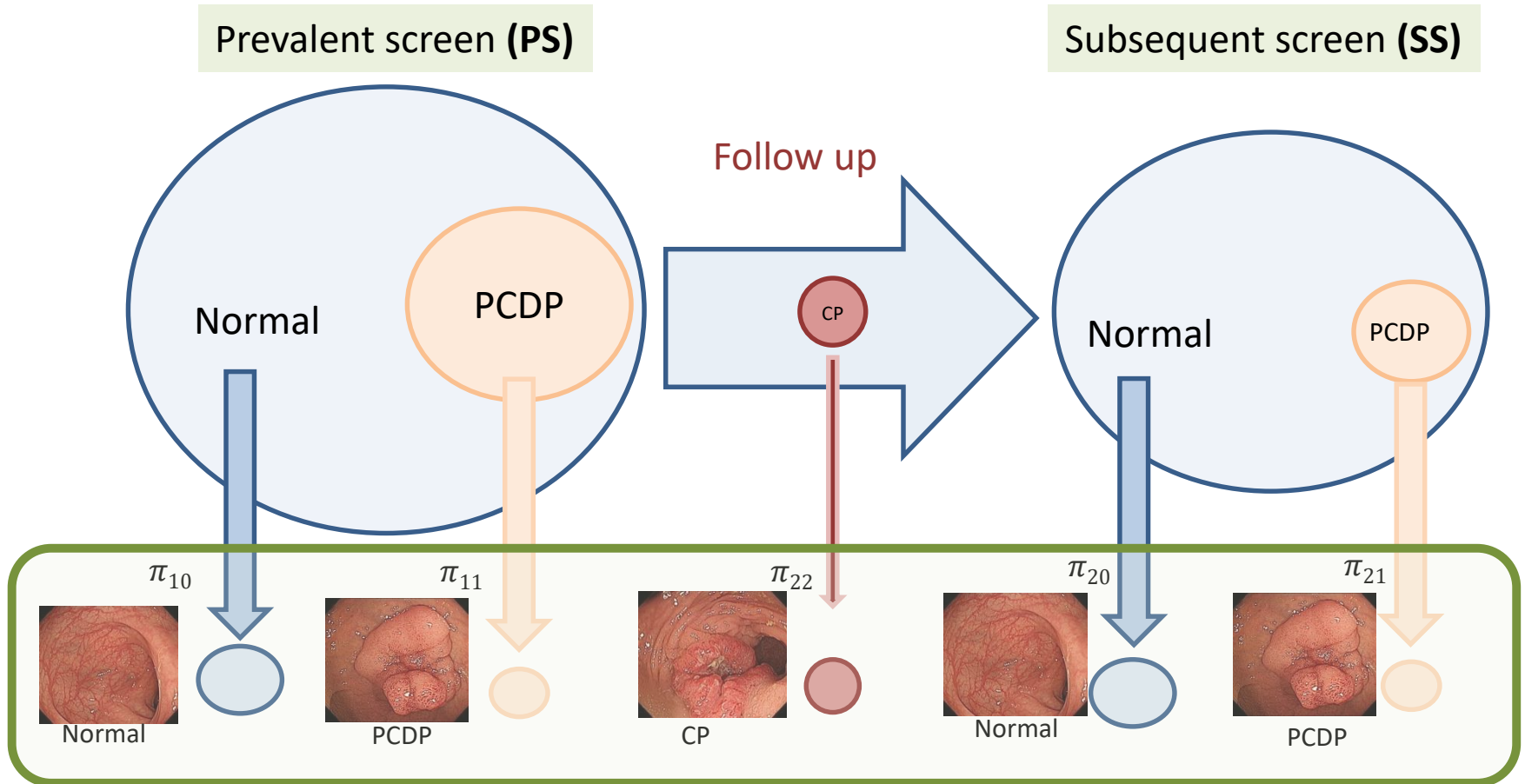
Statistical Characteristics

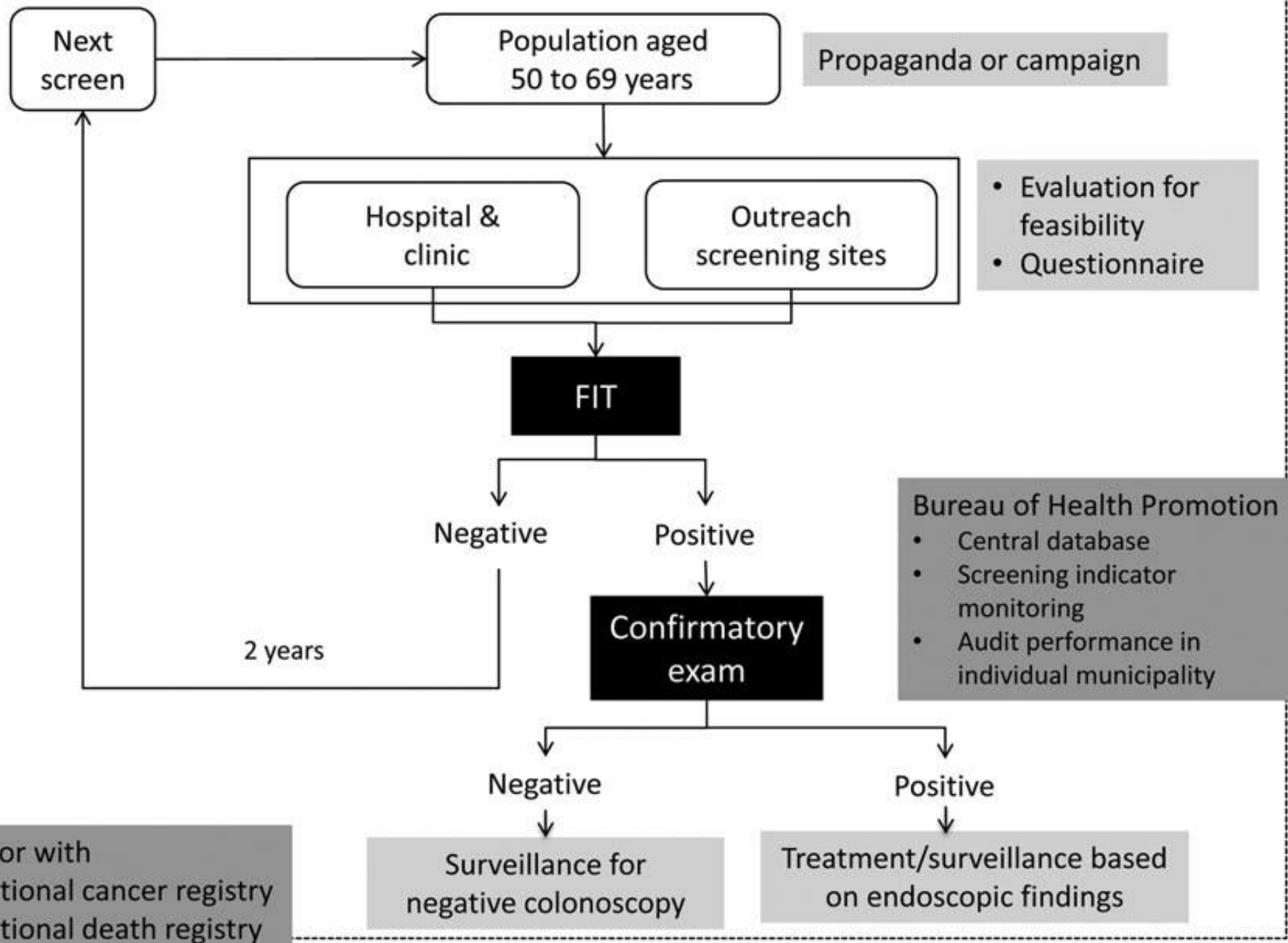
- **Two-stage sampling design for multistate outcome**
 - Normal, **Pre-Clinical Detectable Phase**, **Clinical Phase**



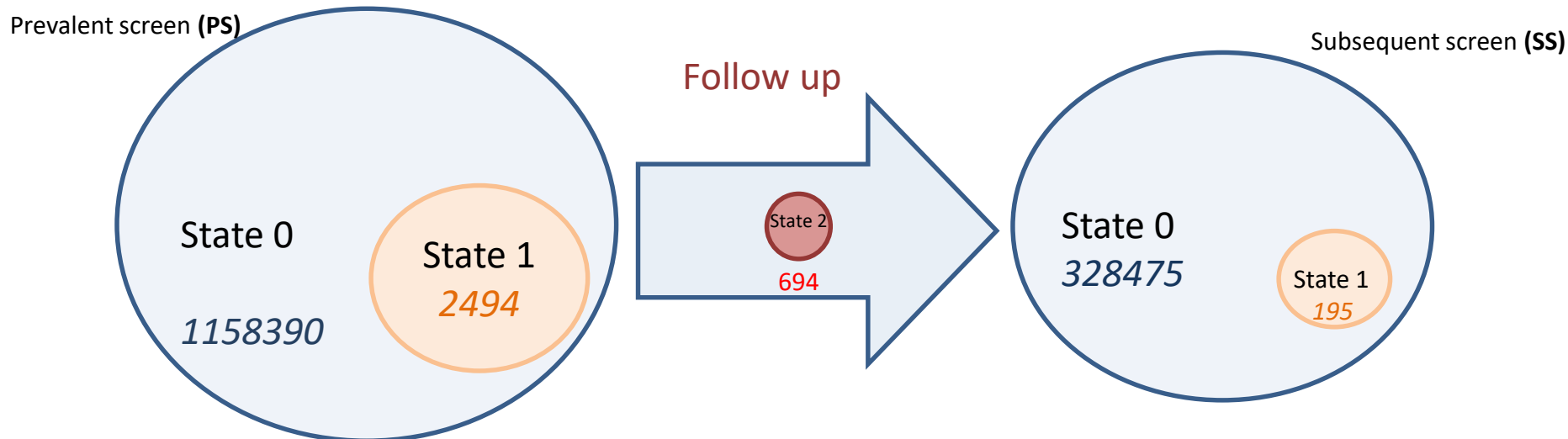
- **Incomplete information**
 - **Prevalent screening round**
 - Left Truncation
 - **Cases detected in subsequent screening round**
 - Interval Censoring
 - **Surface to clinical phase between screen rounds (CP)**
 - Uncensored
- **Measurement error**

Two-stage sampling design for multistate screening data

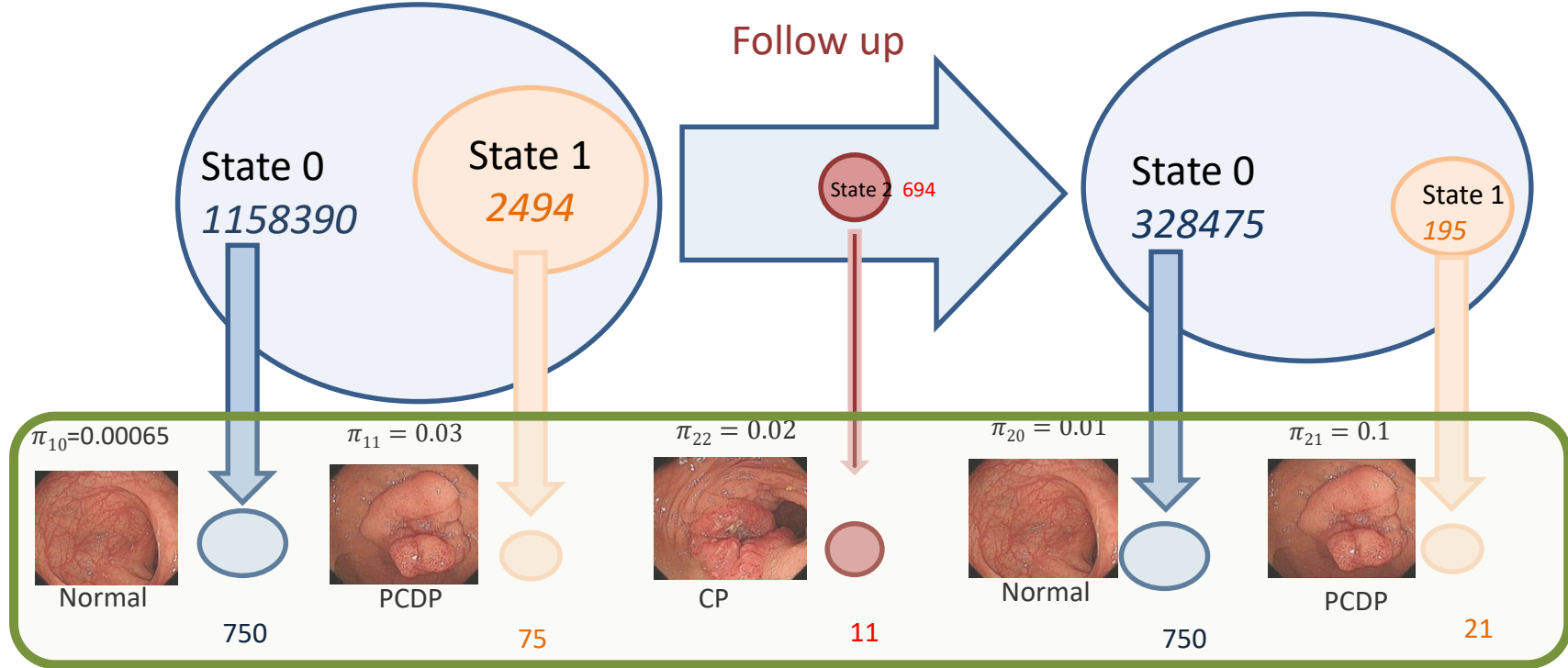




Data on population-based screening for colorectal cancer in Taiwan



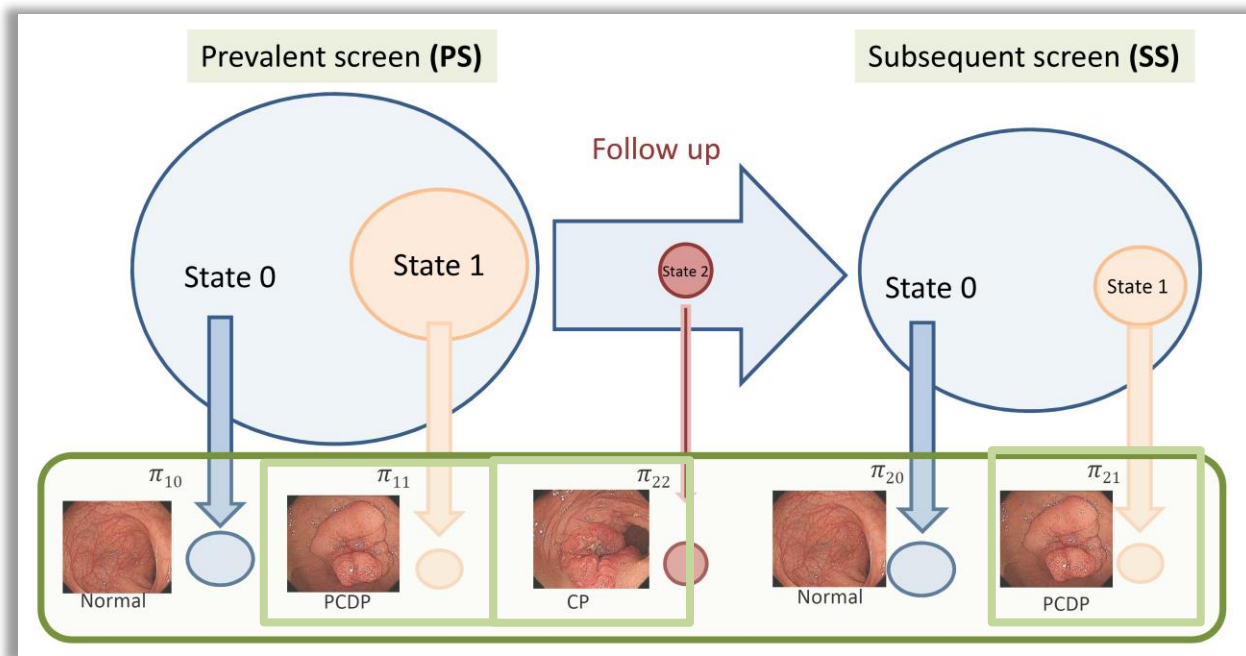
	Normal		PCDP		Interval cancer	
	Frequency	(%)	Frequency	(%)	Frequency	(%)
<i>Prevalent screen</i>						
Overall	1158390	(99.8)	2494	(0.2)	-	-
Male	444937	(38.4)	1347	(54.0)	-	-
Age \geq 60	442793	(38.2)	1424	(57.1)	-	-
<i>Subsequent screen</i>						
Overall	328475	(99.7)	195	(0.06)	694	(0.21)
Male	110862	(33.8)	99	(50.8)	340	(49.0)
Age \geq 60	168966	(51.4)	130	(66.7)	214	(30.8)



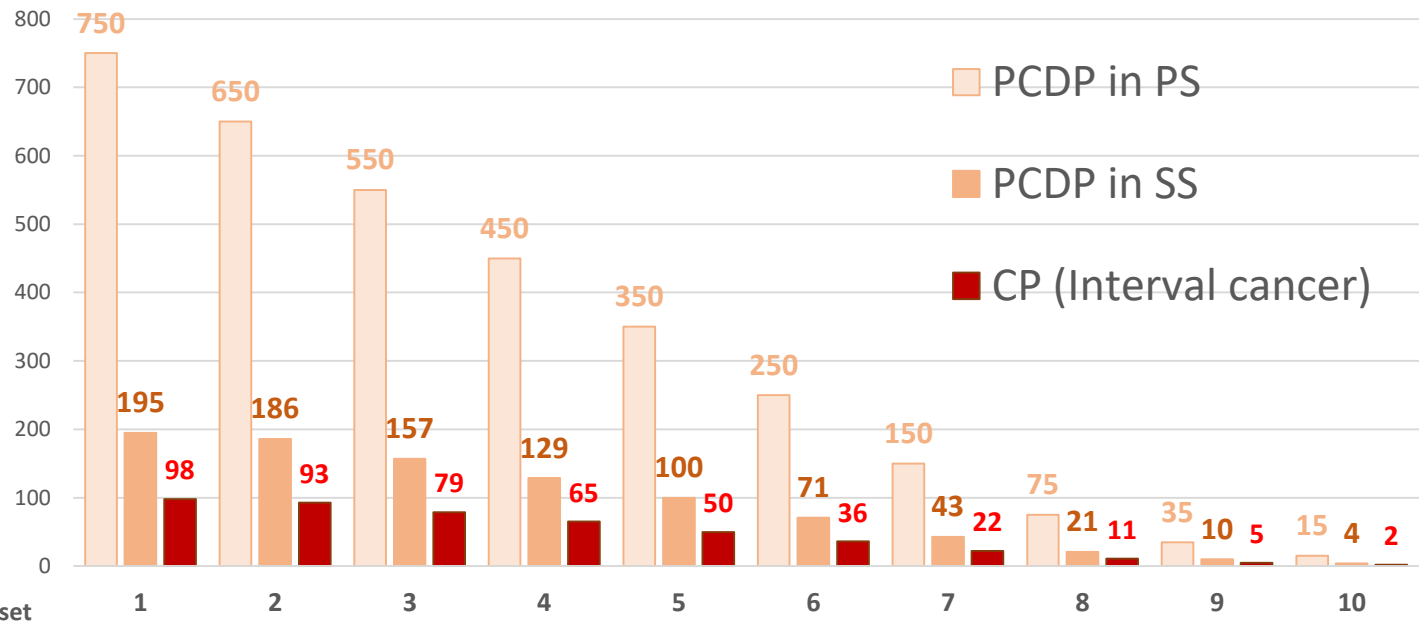
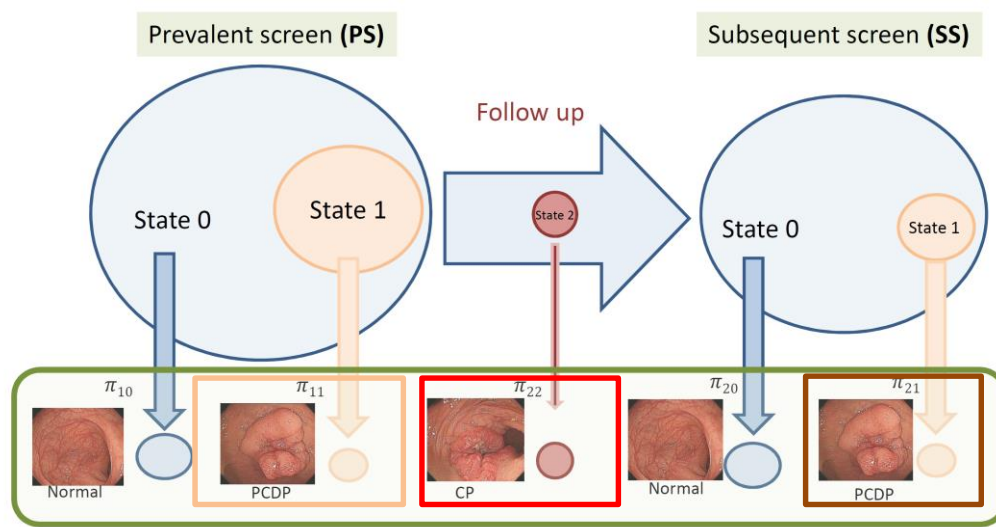
	Full date		Sampling Data set	
$\lambda_1 = \lambda_{40} \exp\{\beta_{11}sex + \beta_{12}(age\ group)\}$,	Normal Subject in PS: 1158390		Normal subject in PS: 750 ($\pi_{10}=0.00065$)	
$sex = \begin{cases} 1, & \text{if male} \\ 0, & \text{otherwise} \end{cases}$,	Normal Subject in SS: 328475		Normal subject in SS: 750 ($\pi_{20}=0.01$)	
$age\ group = \begin{cases} 1, & \text{if } \geq 60\ \text{years} \\ 0, & \text{otherwise} \end{cases}$.	PCDP case in PS: 2494		PCDP case in PS: 75 ($\pi_{11}=0.03$)	
	PCDP in SS: 195		PCDP case in SS: 21 ($\pi_{21}=0.1$)	
	Interval cancer cases: 694		Interval cancer cases: 11 ($\pi_{22}=0.02$)	
Parameter	Estimate	(SD)	Estimate	(SD)
λ_{10}	0.00043	(0.00004)	0.00057	(0.00013)
λ_{20}	0.32	(0.018)	0.33	(0.065)
β_1 (Male vs Female)	0.51	(0.076)	0.54	(0.200)
β_2 (Age ≥ 60 vs <60)	0.67	(0.080)	0.70	(0.205)
Sensitivity	0.81	(0.026)	0.82	(0.081) ¹¹

The influence of sample size on estimated effect of covariate

- Evaluating the effect of sample size on estimated results of covariate effect
 - Reduce sample size of screen detected cases (π_{11}, π_{21})
 - Reduce sample size of interval cancers (π_{22})

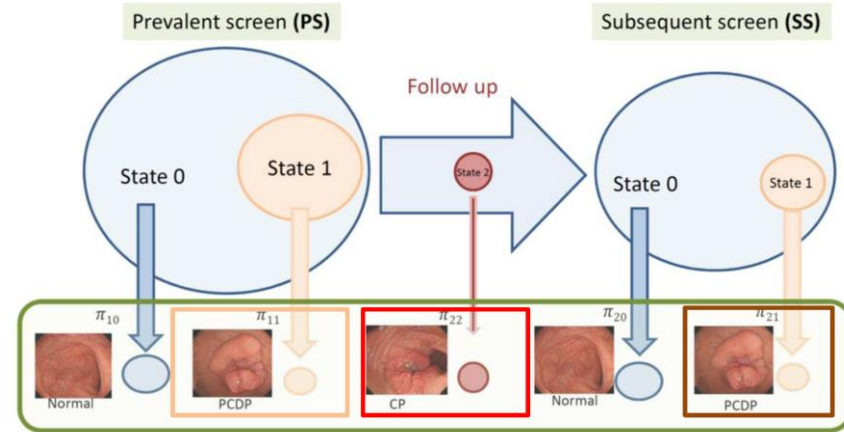
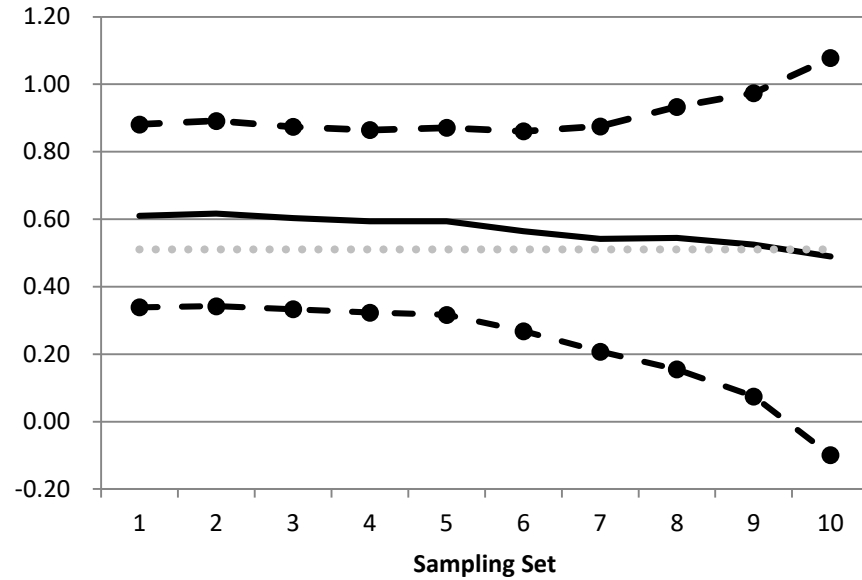


Normal subjects in PS: 750
 ($\pi_{10}=0.00065$)
 Normal subjects in SS: 1500
 ($\pi_{20}=0.0005$)

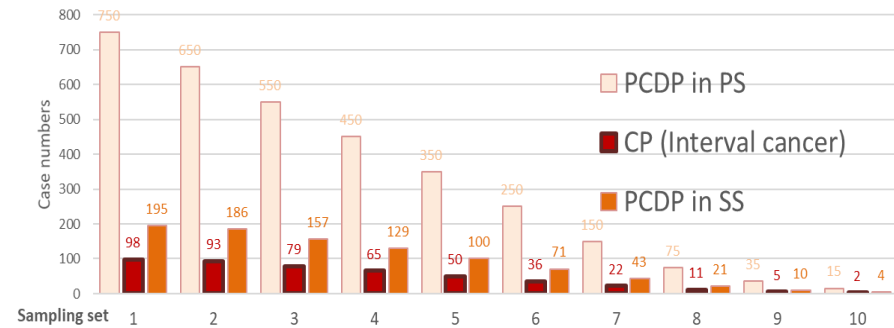
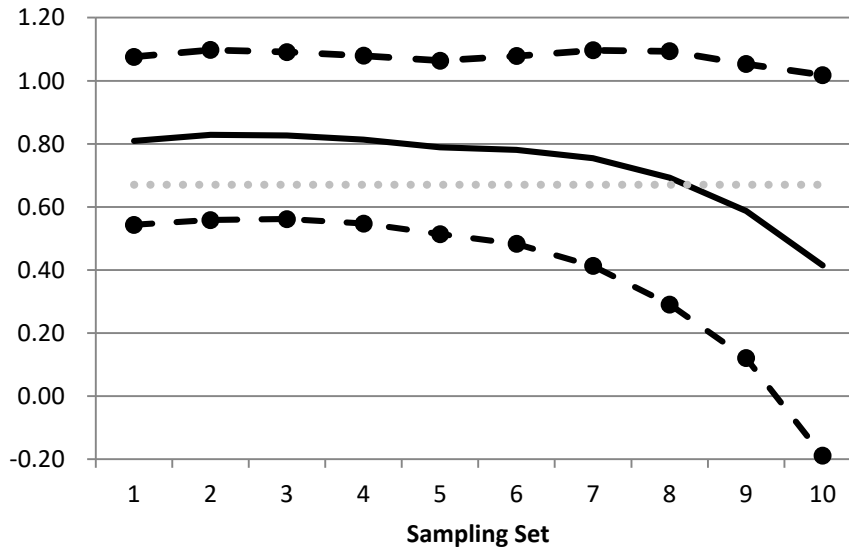


Sampling fraction	$PCDP, PS (\pi_{11})$	$PCDP, SS (\pi_{21})$	$CP (\pi_{22})$
$PCDP, PS (\pi_{11})$	0.30	0.26	0.22
$PCDP, SS (\pi_{21})$	1	0.95	0.81
$CP (\pi_{22})$	0.14	0.13	0.11

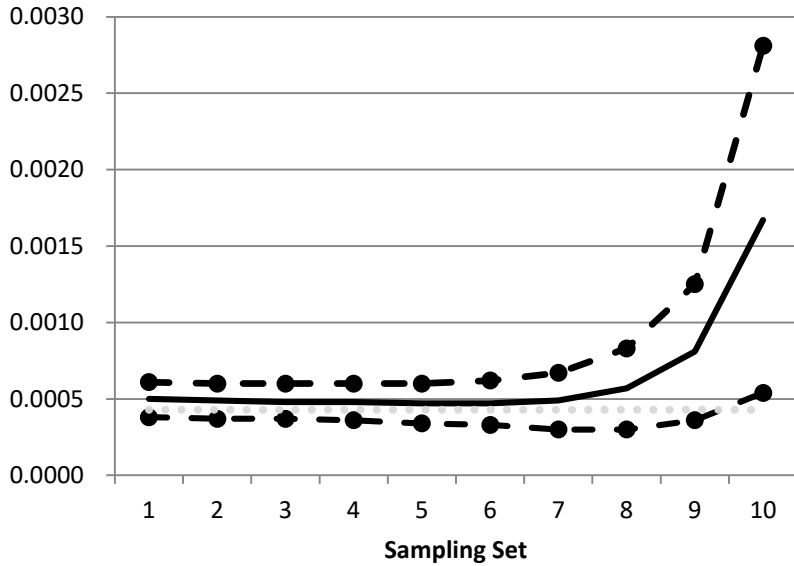
Sex



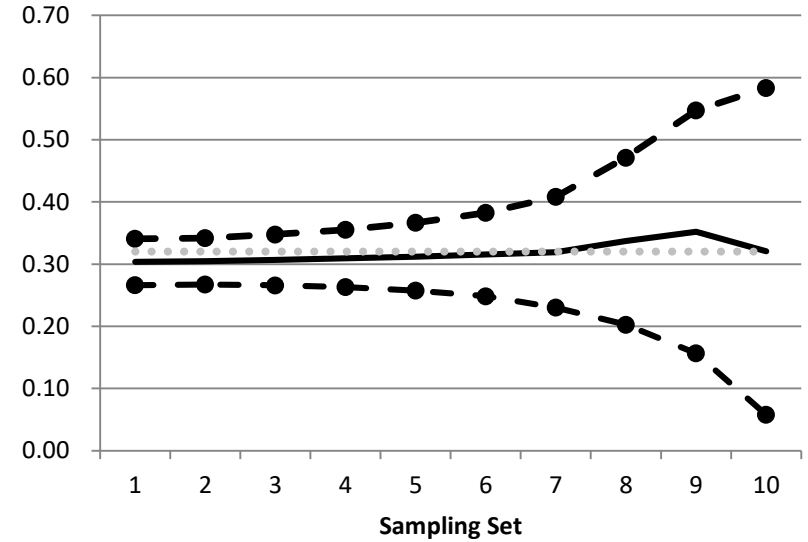
Age



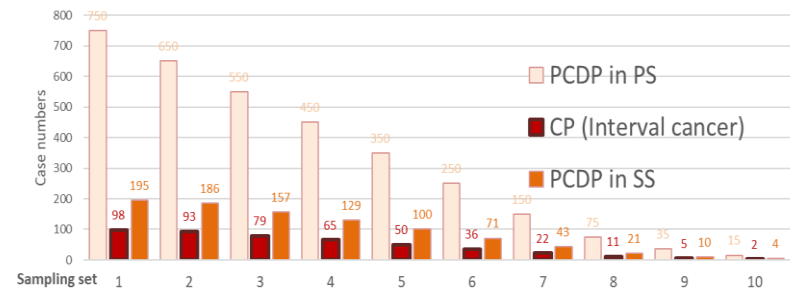
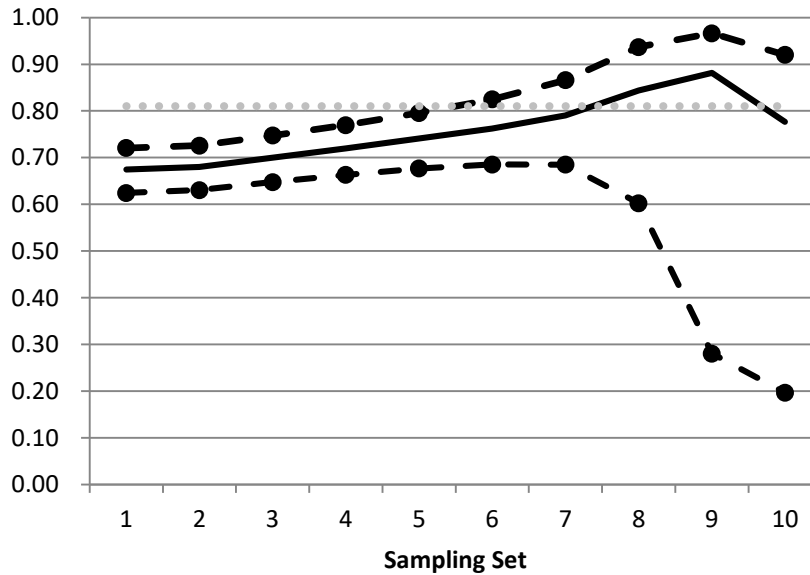
Incidence rate



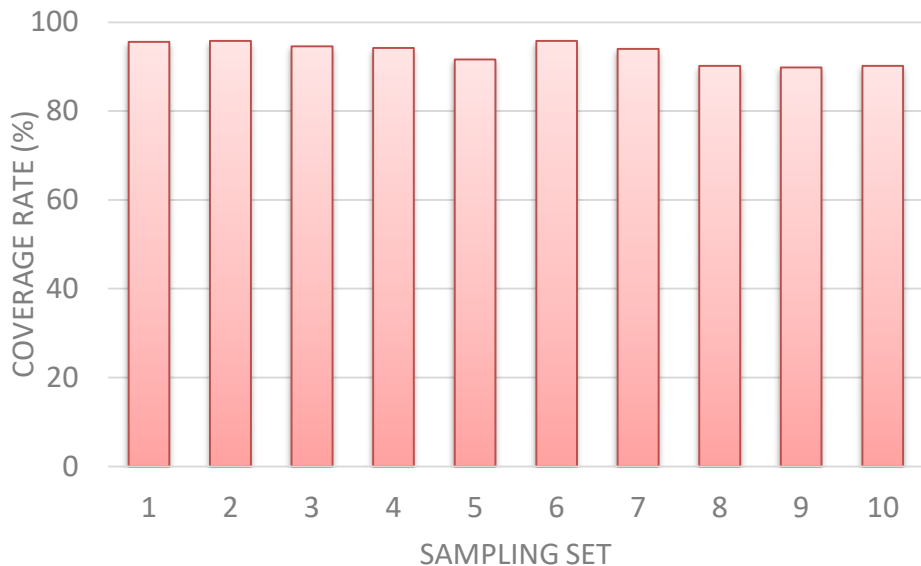
Progress rate



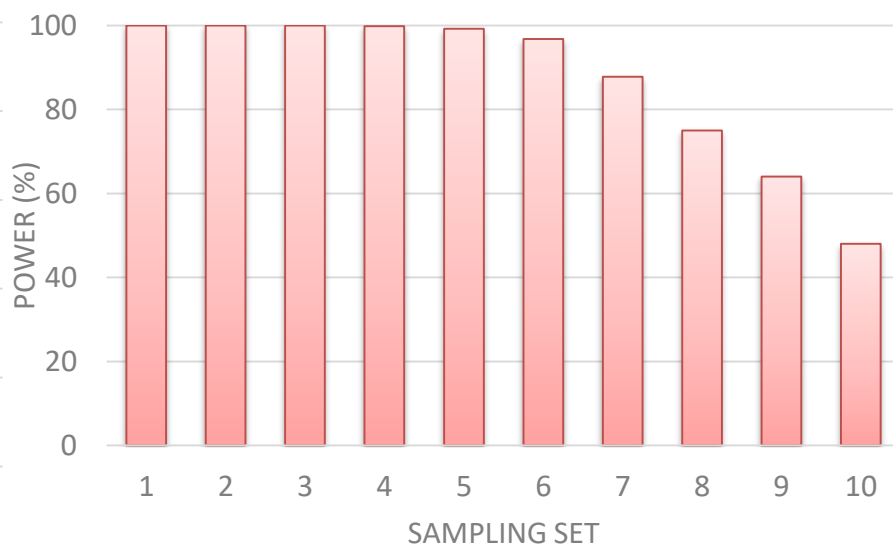
Sensitivity



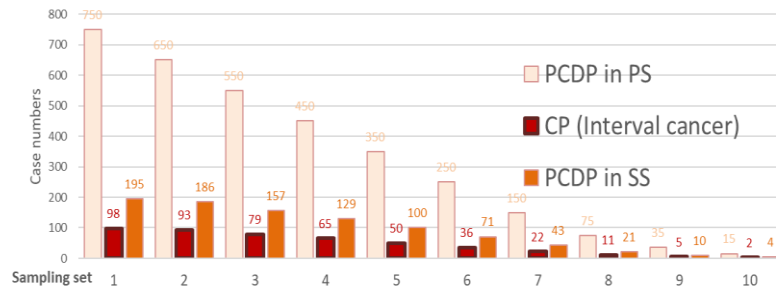
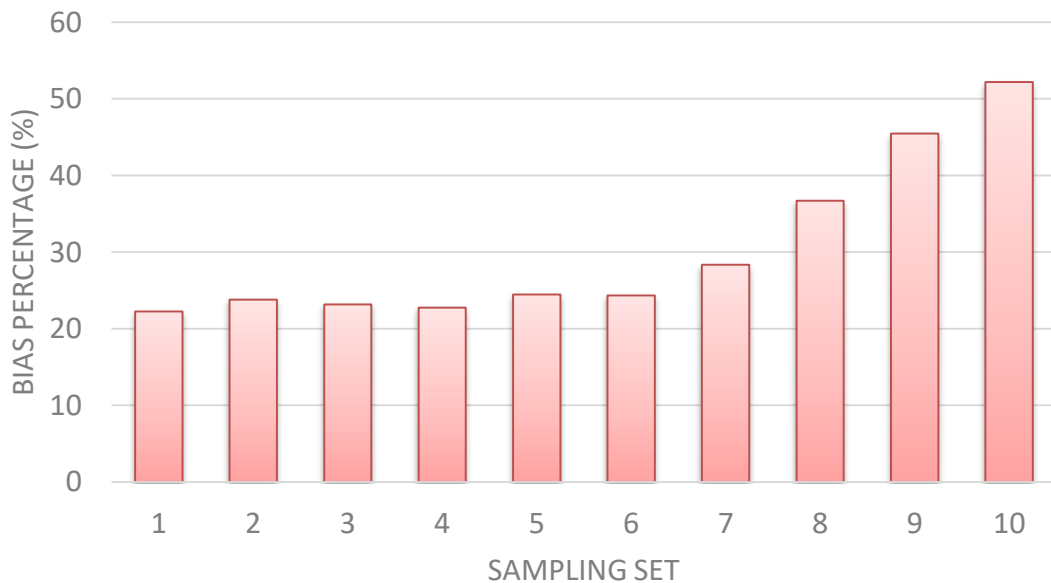
Coverage rate, Sex



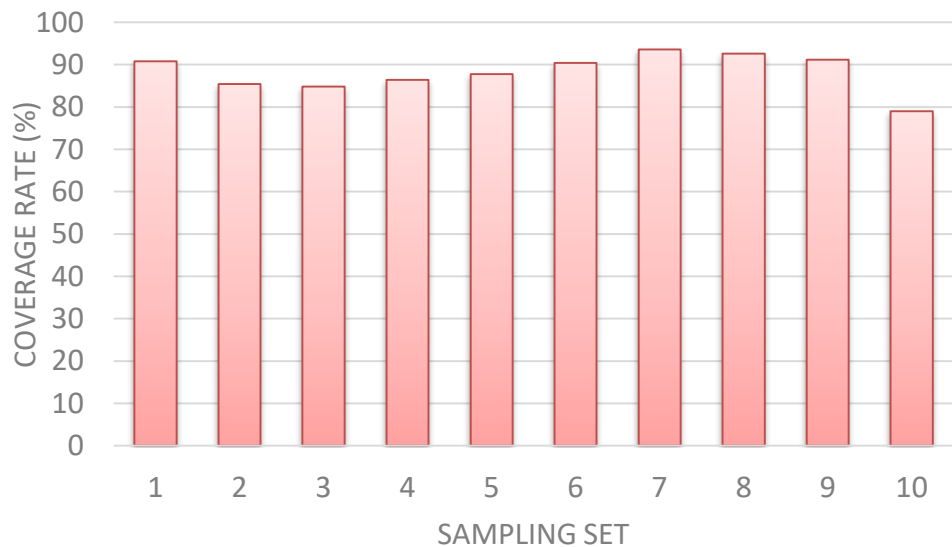
Statistical power, Sex



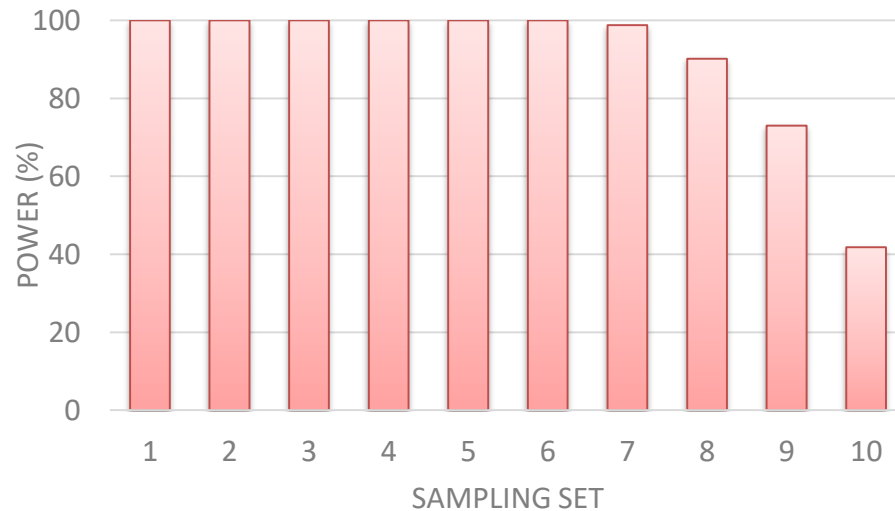
Bias percentage, Sex



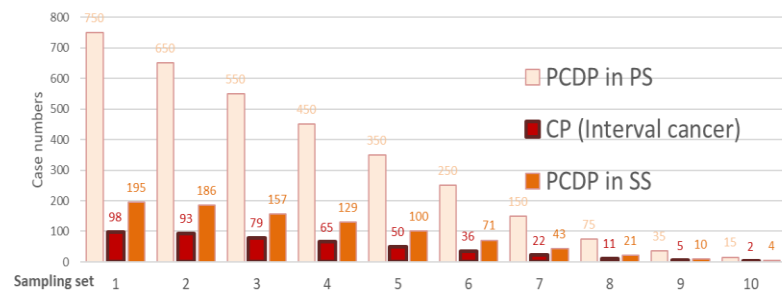
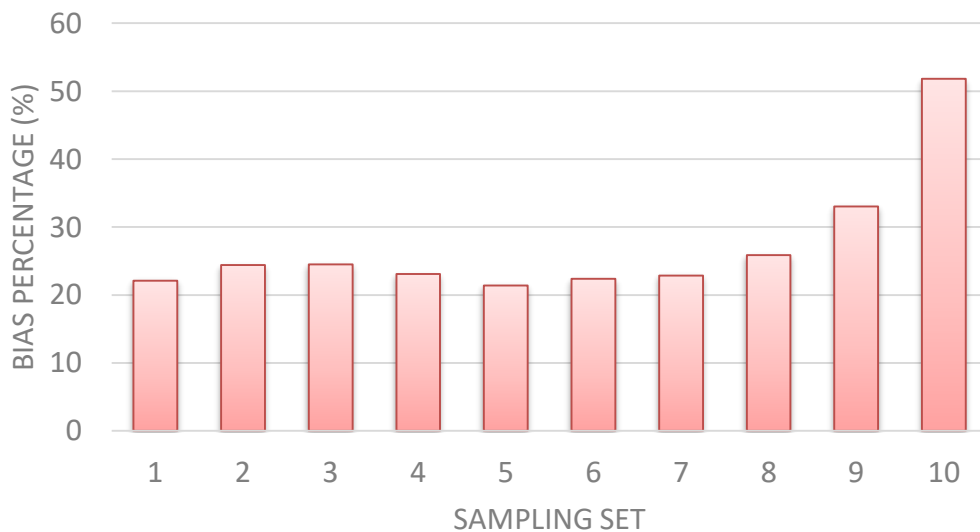
Coverage rate, Age



Statistical power, Age



Bias percentage, Age



Summary

- Two-stage sampling design with multistate outcome
 - Extend the cross-sectional non-standard case-cohort design to longitudinal follow-up data
 - Incorporating measurement error
 - Accommodate the incomplete information (truncation and censoring) characteristics of data
- Assess the state-specific effect of covariates based on sampled data